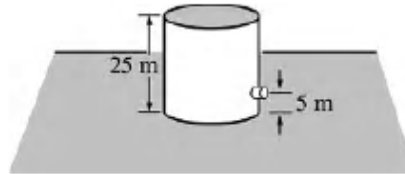


Fizzix AP2 - Greenwichstein High School

Worksheet Thingee

WS 12-1



5. (10 points)

A large tank, 25 m in height and open at the top, is completely filled with saltwater (density 1025 kg/m³). A small drain plug with a cross-sectional area of $4.0 \times 10^{-5} \text{ m}^2$ is located 5.0 m from the bottom of the tank.

The plug breaks loose from the tank, and water flows from the drain.

- Calculate the force exerted by the water on the plug before the plug breaks free.
- Calculate the speed of the water as it leaves the hole in the side of the tank.
- Calculate the volume flow rate of the water from the hole.

$$\begin{aligned} a) \quad P &= P_{\text{ATM}} + \rho gh \\ &= (1 \times 10^5 \text{ Pa}) + (1025)(10)(20) \\ P &= 3.1 \times 10^5 \text{ Pa} \\ F &= PA = (3.1 \times 10^5)(4 \times 10^{-5}) \\ \boxed{F = 12 \text{ N}} \end{aligned}$$

$$\begin{aligned} c) \quad \frac{V}{t} &= nA \\ &= (20 \text{ m/s})(4 \times 10^{-5} \text{ m}^2) \\ \boxed{\frac{V}{t} = 8 \times 10^{-4} \frac{\text{m}^3}{\text{s}}} \end{aligned}$$

$$\begin{aligned} b) \quad \text{Bernoulli @ TOP \& DRAIN} \\ P_{\text{TOP}} + \rho g y_{\text{TOP}} + \frac{1}{2} \rho v_{\text{TOP}}^2 &= P_{\text{DRAIN}} + \rho g y_{\text{DRAIN}} + \frac{1}{2} \rho v_{\text{DRAIN}}^2 \\ P_{\text{TOP}} = P_{\text{DRAIN}} = P_{\text{ATM}} \quad \& \quad v_{\text{TOP}} = 0 \\ \text{so: } \rho g y_{\text{TOP}} &= \rho g y_{\text{DRAIN}} + \frac{1}{2} \rho v_{\text{DRAIN}}^2 \\ \frac{1}{2} \rho v_{\text{DRAIN}}^2 &= \rho g (y_{\text{TOP}} - y_{\text{DRAIN}}) \\ v_{\text{DRAIN}} &= \sqrt{2gh} = \sqrt{2(10)(20)} \\ \boxed{v_{\text{DRAIN}} = 20 \text{ m/s}} \end{aligned}$$